

Page 441, 1

(a) for $\theta \leq 1.5$,

$$\pi(\theta) = 1$$

otherwise

$$\pi(\theta) = \left(\frac{1.5}{\theta}\right)^n$$

(b)

$$\alpha = \max_{\Omega_0} \pi(\theta) = \left(\frac{3}{4}\right)^n$$

Page 441, 2

(a)

$$\begin{aligned}\pi(0) &= 1 \\ \pi(.1) &= .3941 \\ \pi(.2) &= .1558 \\ \pi(.3) &= .3996 \\ \pi(.4) &= .7505 \\ \pi(.5) &= .9423 \\ \pi(.6) &= .9935 \\ \pi(.7) &= .9998 \\ \pi(.8) &= 1 \\ \pi(.9) &= 1 \\ \pi(1) &= 1\end{aligned}$$

(b)

$$\alpha = \pi(.2) = .1558$$

Page 441, 3

accept H_0 when $|\bar{X}_n - \mu_0| < c$.

$$\begin{aligned}0.05 = \alpha &= P(|\bar{X}_n - \mu_0| \geq c) \\ &= P(|Z| \geq 5c) \\ &= 2(1 - \Phi(5c)) \\ c &= \frac{1.96}{5} = 0.392\end{aligned}$$

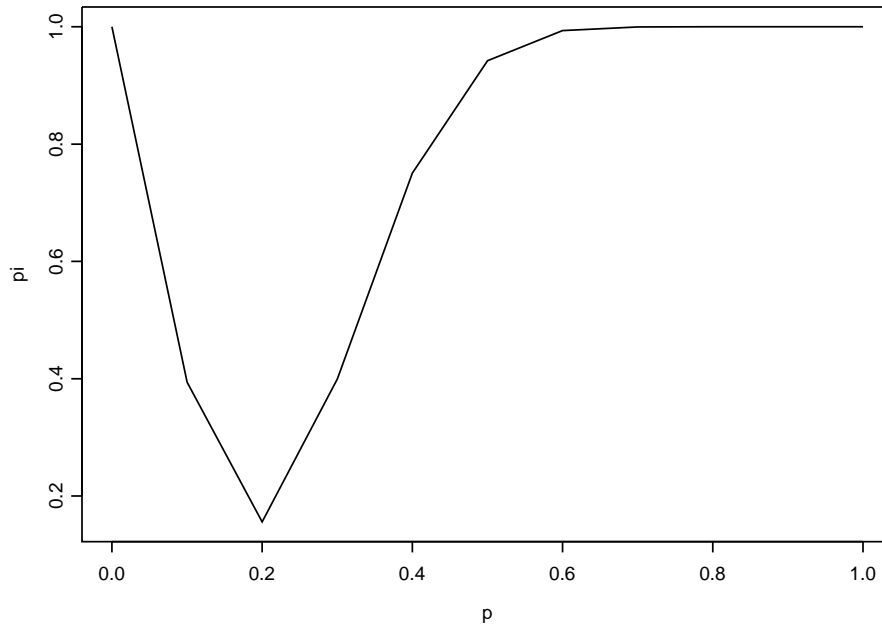


Figure 1: The plot of pi

Page 452, 11

$$P(f_0|x) = \frac{(\frac{2}{3})1}{(\frac{2}{3})1 + (\frac{1}{3})4x^3} = \frac{1}{1 + 2x^3}$$

Expected loss if we guess f_0 :

$$0 \cdot \frac{1}{1 + 2x^3} + 4 \cdot \frac{2x^3}{1 + 2x^3} = \frac{8x^3}{1 + 2x^3}$$

Expected loss if we guess f_1 :

$$1 \cdot \frac{1}{1 + 2x^3} + 0 \cdot \frac{2x^3}{1 + 2x^3} = \frac{1}{1 + 2x^3}$$

So we guess f_0 if

$$\frac{8x^3}{1 + 2x^3} \leq \frac{1}{1 + 2x^3}$$

$$0 < x \leq \frac{1}{2}$$

Page 452, 14

$$P(\text{minor}|x) = \frac{(.8)3^{\sum X_j} e^{-3n}}{(.8)3^{\sum X_j} e^{-3n} + (.2)7^{\sum X_j} e^{-7n}}$$

$$= \frac{(4)3^{\sum X_j}}{(4)3^{\sum X_j} + 7^{\sum X_j} e^{-4n}}$$

Expected loss if we guess minor:

$$2500 \frac{7^{\sum X_j} e^{-4n}}{(4)3^{\sum X_j} + 7^{\sum X_j} e^{-4n}}$$

Expected loss if we guess major:

$$400 \frac{(4)3^{\sum X_j}}{(4)3^{\sum X_j} + 7^{\sum X_j} e^{-4n}}$$

We choose minor if

$$2500 \cdot 7^{\sum X_j} e^{-4n} \leq 1600 \cdot 3^{\sum X_j}$$

$$\sum X_j \leq \frac{\log(\frac{25}{16}) - 4n}{\log(\frac{3}{7})}$$

Problem 3

(a)

$$P(\theta = 1|x) = \frac{e^{-n}}{e^{-n} + e^{-4n} 4^{\sum X_j}}$$

$$= \frac{1}{1 + 4^{\sum X_j} e^{-3}}$$

(b)

$$L_x(\theta) \propto e^{-5\theta} \theta^{24}$$

$$r(x) = \frac{L_x(4)}{L_x(1)} = e^{-15} 4^{24}$$

(c) $\sum_{j=1}^5 X_j$ is the sufficient statistics. $\sum X_j$ is distributed approximately normal $N(5, 5)$.

$$P(\sum X_j > 24 | \theta = 1) \approx P(z > \frac{24 - 5}{\sqrt{5}}) = 0$$

Or in S-plus,

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1-ppois(24, 5)
> 1.6 e-10
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