

# **Extrasensory Perception**

• One way to test for ESP is with Zener cards:



 Subjects draw a card at random and telepathically communicate this to someone who then guesses the symbol

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**Extrasensory Perception** 

- There are five cards with five different symbols
- If there is no such thing as ESP, what proportion of guesses should be correct?



Because there are 5 cards, each person has a 1/5 chance of guessing correctly each time, if ESP does not exist.

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**Extrasensory Perception** 

- As we've learned, statistics vary from sample to sample
- Even if the population proportion is 1/5, not every sample proportion will be exactly 1/5
- How do we determine when a sample proportion is far enough above 1/5 to provide evidence of ESP?

## **Statistical Test**

A *statistical test* uses data from a sample to assess a claim about a population

• In the ESP experiment, we want to use sample data to determine whether the population proportion of correct guesses is really higher than 1/5



### **Statistical Evidence**

- Let  $\hat{p}$  denote the sample proportion of correct guesses in an ESP experiment
- Which of these sample statistics would give the strongest evidence for ESP?

a)  $\hat{p} = 0$ b)  $\hat{p} = 1/5$ c)  $\hat{p} = 1/2$ d)  $\hat{p} = 3/4$ 

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3/4 is the highest, so provides the strongest evidence of ESP.



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# 😥 Extrasensory Perception

- Let's create our own sample proportion!
- Randomly choose a letter from A B C D E, and write it down (don't show anyone!)
- Find a partner, telepathically communicate your letter (no auditory or visual clues!), and have them guess your letter. Switch roles.
- Did you guess correctly?
  - a) Yes
  - b) No

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# Extrasensory Perception

- What is the sample proportion for our class?
- This provides
  - a) Strong evidence for ESP
  - b) Weak evidence for ESP
  - c) No evidence for ESP
  - d) Not sure
- Next class, we'll learn how to quantify this evidence!

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### **Statistical Hypotheses**

• Statistical tests are framed formally in terms of two competing hypotheses:

*Null Hypothesis (H<sub>0</sub>):* Claim that there is no effect or difference.

*Alternative Hypothesis (H<sub>a</sub>):* Claim for which we seek evidence.

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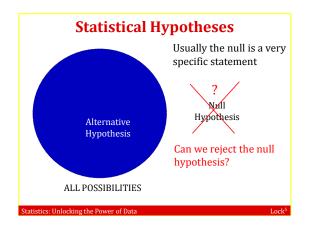
# Statistical Hypotheses

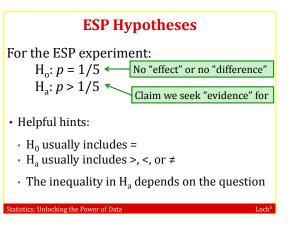
H<sub>o</sub>: Null hypothesis

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Competing claims about a population

- H<sub>a</sub>: Alternative hypothesis
- population
- The alternative hypothesis is established by observing evidence (data) that contradicts the null hypothesis and supports the alternative hypothesis
- Hypotheses are always about population parameters





#### **Sleep versus Caffeine**



- Students were given words to memorize, then randomly assigned to take either a 90 min nap, or a caffeine pill. 2 ½ hours later, they were tested on their recall ability.
- · Explanatory variable: sleep or caffeine
- Response variable: number of words recalled
- · Is sleep or caffeine better for memory?

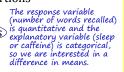
Mednick, Cai, Kanady, and Drummond (2008), "Comparing the benefits of caffeine, naps and placebo on verbal, motor and perceptual memory," *Behavioral Brain Research*, 193, 79-86. Statistics: Unlocking the Power of Data Lock



#### **Sleep versus Caffeine**

What is the parameter of interest in the sleep versus caffeine experiment?

- a) Proportion
- b) Difference in proportions
- c) Mean (d) Difference in means e) Correlation



**Sleep versus Caffeine** 

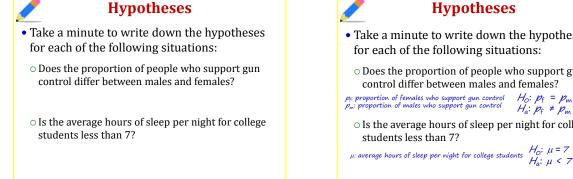
- Let  $\mu_s$  and  $\mu_c$  be the mean number of words recalled after sleeping and after caffeine.
- Is there a difference in average word recall between sleep and caffeine?
- What are the null and alternative hypotheses?

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#### **Difference in Hypotheses**

• Note: the following two sets of hypotheses are equivalent, and can be used interchangeably:

$$\begin{array}{ll} H_0: \, \mu_1 = \mu_2 & H_0: \, \mu_1 - \mu_2 = 0 \\ H_a: \, \mu_1 \neq \mu_2 & H_a: \, \mu_1 - \mu_2 \neq 0 \end{array}$$





 Take a minute to write down the hypotheses for each of the following situations:

 $\odot$  Does the proportion of people who support gun control differ between males and females?

 $H_0: p_f = p_m$  $H_a: p_f \neq p_m$ 

○ Is the average hours of sleep per night for college

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#### **Your Own Hypotheses**

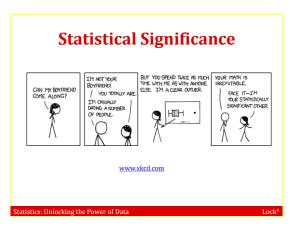
- · Come up with a situation where you want to establish a claim based on data
- What parameter(s) are you interested in?
- · What would the null and alternative hypotheses be?
- What type of data would lead you to believe the null hypothesis is probably not true?

# Statistical Significance

When results as extreme as the observed sample statistic are *unlikely* to occur by random chance alone (assuming the null hypothesis is true), we say the sample results are *statistically significant* 

- If our sample is statistically significant, we have convincing evidence against  $H_0$ , in favor of  $H_a$
- If our sample is not statistically significant, our test is inconclusive

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#### Note on Statistical Significance

- Statistical significance is a difficult concept, but also one of the most fundamental concepts of the course
- We return to this concept almost every class for the rest of the semester, so

oit will get easier!

oit's worth thinking deeply about!

#### **Extrasensory Perception**

p = Proportion of correct guesses  $H_0: p = 1/5$  $H_a: p > 1/5$ 



- If results are statistically significant...
  - $\circ$  the sample proportion of correct guesses is higher than is likely just by random chance (if ESP does not exist and p = 1/5)
  - we have evidence that the true proportion of correct guesses really is higher than 1/5, and thus have evidence of ESP

**Extrasensory Perception** 

p = Proportion of correct guesses H<sub>0</sub>: p = 1/5



- If results are NOT statistically significant...
  - the sample proportion of correct guesses could easily happen just by random chance (if ESP does not exist and p = 1/5)
  - $\circ$  we do not have enough evidence to conclude that p > 1/5, or that ESP exists

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 $H_{a}: p > 1/5$ 



#### **Sleep versus Caffeine**

 $\mu_s$  and  $\mu_c$ : mean number of words recalled after sleeping and after caffeine

 $H_0: \mu_s = \mu_c, H_a: \mu_s \neq \mu_c$ 

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The sample difference in means is  $\bar{x}_s - \bar{x}_c = 3$ , and this is statistically significant. We can conclude...

a) there is a difference between sleep and caffeine for memory (and data show sleep is better)
b) there is not a difference between sleep and caffeine for memory
c) nothing

#### Summary

- Statistical tests use data from a sample to assess a claim about a population
- Statistical tests are usually formalized with competing hypotheses:
- $\circ$  Null hypothesis (H\_0): no effect or no difference  $\circ$  Alternative hypothesis (H\_a): what we seek evidence for
- If it would be unusual to get results as extreme as that observed, just by random chance, if the null were true, then the data is statistically significant
- If data are statistically significant, we have convincing evidence against the null hypothesis, and in favor of the alternative

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#### To Do

- Read Section 4.1
- Do Homework 3 (due Tuesday, 9/25)
- Idea and data for **Project 1** (proposal due 9/27)