

STA 110

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Fall 1995 **Name:** \_\_\_\_\_

### Quiz 4 (Ver 2)

**Bolts.** A machine produces bolts which are 20% defective. Find the probability that in a random sample of 400 bolts produced by this machine (a) at most 100, (b) between 70 and 90, (c) 85 or more, of the bolts will be defective.

**Example:** When you roll a fair die once you expect 3.5 points with a standard deviation of 1.708. (Variance 2.918).

Estimate the probability that in 1000 rollings the total sum will be between 3500 and 3600 points.

**Gain in a long run.** The gain in a game is described by

$X$	-1	0	5
$p$	0.2	0.2	0.6

(a) Would you play the game? Explain.

(b) If you play the game 100 times what are the chances of ending with a negative balance?

[Sol.  $EX = 2.8, VarX = 7.36, \sigma X = 2.71, S = X_1 + \dots + X_{100}, S$  is approx. normal (CLT),  $ES = 280, VarS = 736, \sigma S = 27.1, P(S < 0) = P(Z < \frac{0-280}{27.1}) = P(Z < -10.33) = 0.$ ]