

13-8

- a. Note that $df = 66 - 3 - 1 = 62 \approx 60$, so $t_{.025} = 2$.

X_1

$$95\% \text{ CI} = 0.021 \pm 2 \cdot 0.019 = 0.021 \pm 0.38$$

$$t\text{-ratio} = 0.021/0.019 = 1.105$$

$$p\text{-value} > 2 \cdot 0.1 = 0.2 \text{ (two-sided } p\text{-value)}$$

X_2

$$95\% \text{ CI} = 0.075 \pm 2 \cdot 0.034 = 0.075 \pm 0.068$$

$$t\text{-ratio} = 0.075/0.034 = 2.206$$

$$p\text{-value } 2 \cdot 0.010 = 0.02, \text{ ie, } 0.02 - -0.05 \text{ (two-sided } p\text{-value)}$$

X_3

$$95\% \text{ CI} = 0.043 \pm 2 \cdot 0.018 = 0.043 \pm 0.036$$

$$t\text{-ratio} = 0.043/0.018 = 2.390$$

$$p\text{-value} \approx 2 \cdot 0.010 = 0.02 \text{ (two-sided } p\text{-value)}$$

- b. We are assuming that the 66 students are a random sample for a hypothetical large population, which in this case is not so reasonable – they are very far from having been selected at random, they are just the available students at a certain time.
- c. The variable X_3 , because it has the largest t -ratio and smallest p -value.
- d. We should keep the first regressor first because there is enough statistical evidence to support that, and second because it is very reasonable to expect that a student's rank (from the bottom) is positively related with his/her score in a test.

13-11

- a. $\Delta Y = b_2 \Delta X_2 = -1.1(5 - 2) = -3.3$, therefore the answer should be less \$3.3 per front foot.
- b. $\Delta Y = b_3 \Delta X_3 = -1.34(-1/2) = 0.67$, and we conclude that the price per front foot is \$0.67 higher if the lot is $1/2$ a mile closer to the nearest paved road (other things being equal).
- c. $\Delta Y = b_1 \Delta X_1 = 1.5(5 - 1) = 6$, so the price is \$6 per front foot higher than in 1970. (Same kind of lot: size and distance from the nearest paved road.)

14-3

- a. $df = 1072 - 5 - 1 = 1066 \Rightarrow t_{.025} \approx z_{.025} = 1.96$

AGE	$-3.9 \pm 1.96 \times 1.8 = -3.9 \pm 3.53$
SMOK	$-9.0 \pm 1.96 \times 2.2 = -9.0 \pm 4.31$
CHEMW	$-350 \pm 1.96 \times 46 = -350 \pm 90.16$
FARMW	$-380 \pm 1.96 \times 53 = -380 \pm 103.88$
FIREW	$-180 \pm 1.96 \times 54 = -180 \pm 105.84$

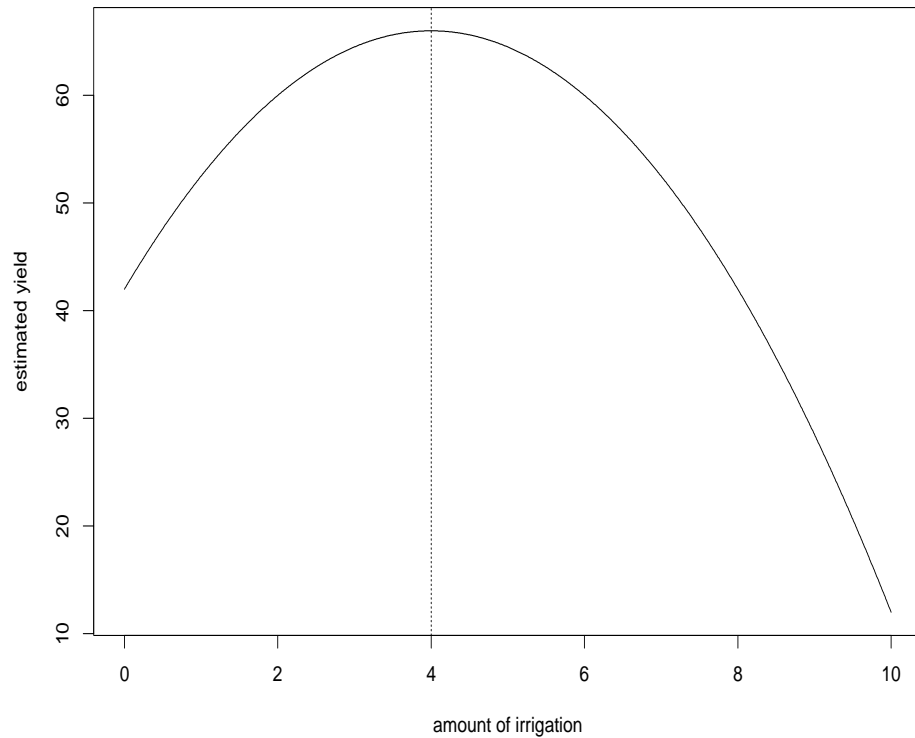
- b. age and amount of cigarettes per day; 9; lower.
- c. 30; higher.
- d. 39; lower.
- e. $20 \times 9 = 180$; lower.
- d. $180/39 \approx 4.6$ years; important variables may be omitted.

14-9

- a.
 - i. $D_A = D_B = 0$, so $\hat{Y} = 61$.
 - ii. $D_A = 1$, $D_B = 0$, so $\hat{Y} = 61 + 9 = 70$.
 - iii. $D_A = 0$, $D_B = 1$, so $\hat{Y} = 61 + 12 = 73$.
- b. \bar{C} = answer i., \bar{A} = answer ii. and \bar{B} = answer iii..
- c. one factor ANOVA; “Yield” is the response, the factor is the type of fertilizer — A, B or none (C).

14-13

- a. Not very credible, since too much water should have a negative effect on the yield.
- b. We should test that the coefficient for I^2 is zero. $df = 14 - 2 - 1 = 11$ and the t ratio is $-1.5/.4 = -3.75$ which implies that the p-value is between $2 \times .001$ and $2 \times .0025$, that is $0.002 < p\text{-value} < 0.005$. This conveys very little evidence in support of this hypothesis, which confirms our previous answer.
- c. The maximum occurs at $I = 4$, but we can use less water without decreasing too much the yield.



d. $\Delta \hat{Y} = 12 \cdot \Delta I - 1.5 \cdot \Delta I^2 = 12 \cdot (3 - 2) - 1.5 \cdot (3^2 - 2^2) = 4.5$

14-18

- a. elasticity = 1.3 (slope)
- b. relative change in price \approx change in log price, so if price increased by 3%, the price changed 0.03. Hence, $\Delta \log Q = 1.3 \times 0.03 = 0.039$ and, for the same reason, we conclude that Q increased by 3.9%
- c. relative change in Q of 10% \approx change in $\log Q$ of 0.1, so,

$$0.1 = 1.3 \Delta \log P \Leftrightarrow \Delta \log P = \frac{0.1}{1.3} = 0.007$$

so that the relative change in price should be approximately 7.7%.