

11-8 (p.369)

(b)

$$\begin{aligned}b &= \frac{\Sigma(X - \bar{X})(Y - \bar{Y})}{\Sigma(X - \bar{X})^2} \\&= \frac{9.1}{18.3} \\&\approx 0.497\end{aligned}$$

$$\begin{aligned}a &= \bar{Y} - b\bar{X} \\&= 5.8 - \frac{9.1}{18.3}(5.8) \\&\approx 2.92\end{aligned}$$

$$\hat{Y} = 2.92 + 0.497X$$

(c) For a father who is 6 feet tall:

i) 6

ii) 5.8

iii) 5.9

For a father who is 5 feet tall:

i) 5

ii) 5.8

iii) 5.4

Choice iii performs best.

(d) less, although still more; not so well, although still better; will not

12-15 (p. 392)

(a)

$$\begin{aligned}b &= \frac{46100}{36400} \approx 1.27 \\a &= 140 - \frac{46100}{36400}(110) \approx 0.687 \\ \hat{Y} &= 0.687 + 1.27X\end{aligned}$$

(c) Prediction for $X=180$.

$$s \approx 29.2$$

$$t_{.025}^4 = 2.78$$

$$229 \pm (2.78)(29.2) \sqrt{\frac{1}{6} + \frac{4900}{36400}}$$

(184 , 274)

(d) Prediction for $X=180$ if last year's had been unavailable.

$$\bar{Y} \pm t_{.025}^{n-1} \frac{s}{\sqrt{n}}$$

$$140 \pm (2.57) \frac{\sqrt{\frac{61800}{5}}}{\sqrt{6}}$$

(23.4 , 257)

(e) Confidence interval in part (c) is much narrower and is centered better.

12-16 (p. 393)

(a) $\Sigma(Y - \hat{Y})^2 \approx 3416$ (used to get s in 12-15c)

(b) If $\hat{Y} = 10 + X$, $\Sigma(Y - \hat{Y})^2 \approx 8400$. Have to recalculate \hat{Y} to do it.

12-18 (p. 393)

(a) The “7”'s which are “out of line” with the others look suspicious.

(b)

$$b = \frac{1222}{113.8} \approx 10.74$$

$$a = 68.2 - \frac{1222}{113.8}(3.46) \approx 31.05$$

$$\hat{Y} = 31.05 + 10.74X$$

(c) $\hat{Y} = a + b(2) \approx 52.52$ So almost 53 minutes later is the prediction for the next eruption.

(d) about 50%

(e)

$$\begin{aligned}
 (a + bX_0) &= t_{.10}^{105} \sqrt{s^2} \sqrt{\frac{1}{n} + \frac{(X_0 - \bar{X})^2}{\Sigma(X - \bar{X})^2} + 1} \\
 (31.05 + (10.74)(2)) &= 1.29\sqrt{44.7} \sqrt{\frac{1}{107} + \frac{(2 - 3.46)^2}{113.8} + 1} \\
 (43.79 \quad , \quad \infty)
 \end{aligned}$$

(f)

$$\begin{aligned}
 (a + bX_0) &= t_{.10}^{105} \sqrt{s^2} \\
 (31.05 + (10.74)(2)) &= 1.29\sqrt{44.7} \\
 (43.91 \quad , \quad \infty)
 \end{aligned}$$

The approximation is about as adequate for $X = 2$ as for $X = 5$, since both are about the same distance away from \bar{X} . The approximations only differ from the answers obtained through the method in part (e) by 0.12, which is about 7.2 seconds.