# ♠ Affymetrix expression data

- See Affymetrix tutorial
- Expression summaries: AD and ALR, and other information
- Array normalisation; Hybridisation problems low levels of intensity

# ♠ One gene: Sample statistics, summaries and exploration

- Sample  $x_1, \ldots, x_n$  of expression on one gene
- Sample mean  $\bar{x} = n^{-1} \sum_{j=1}^{n} x_j$  Sample variances  $s = (n-1)^{-1} \sum_{j=1}^{n} (x_j \bar{x})^2$
- Sample standard deviation (sd or std)  $\sqrt{s}$
- Median, quartiles
- Histograms

# ♠ Multiple genes: Sample statistics, summaries and exploration

- Gene i, i = 1, ..., p
- Expression level  $x_{i,j}$  on array j
- Column vector  $\mathbf{x}_j$  of dimension  $p \times 1$  all genes on array j
- $p \times n$  (tall, skinny) matrix  $\mathbf{X} = [\mathbf{x}_1, \dots, \mathbf{x}_n]$
- Gene i sample summaries  $\bar{x}_i, s_i$
- Sample covariance between genes i, k is  $s_{i,k} = (n-1)^{-1} \sum_{i=1}^{n} (x_{i,i} \bar{x}_i)(x_{k,i} \bar{x}_k)$ note:  $s_{i,i} = s_i$
- Sample correlation between genes i, k is  $r_{i,k} = s_{i,k} / \sqrt{s_i s_k}$ note:  $r_{i,i} = 1$
- Matrix notation: Sample variance (or covariance) matrix  $\mathbf{S} = (s_{i,k})$

$$\mathbf{S} = \begin{pmatrix} s_1 & s_{1,2} & \cdots & s_{1,p} \\ s_{1,2} & s_2 & \cdots & s_{2,p} \\ \vdots & \vdots & \ddots & \vdots \\ s_{1,p} & s_{2,p} & \cdots & s_p \end{pmatrix}$$

- S is  $p \times p$  symmetric, non-negative definite matrix
- Matrix notation: Sample correlation matrix  $\mathbf{R} = (r_{i,k})$

$$\mathbf{R} = \begin{pmatrix} r_{1,1} & r_{1,2} & \cdots & r_{1,p} \\ r_{1,2} & r_{2,2} & \cdots & r_{2,p} \\ \vdots & \vdots & \ddots & \vdots \\ r_{1,p} & r_{2,p} & \cdots & r_{p,p} \end{pmatrix} = \begin{pmatrix} 1 & r_{1,2} & \cdots & r_{1,p} \\ r_{1,2} & 1 & \cdots & r_{2,p} \\ \vdots & \vdots & \ddots & \vdots \\ r_{1,p} & r_{2,p} & \cdots & 1 \end{pmatrix}$$

• **R** is  $p \times p$  symmetric, non-negative definite matrix

# **♠** Matrix notation

• Suppose X has variables all standardised to zero mean; that is,  $\bar{x}_i = 0$  for all genes  $i = 1, \dots, p$ (just subtract a non-zero mean to begin to assure this). Then the variances and covariances simplify,  $s_{i,k} = (n-1)^{-1} \sum_{j=1}^{n} x_{i,j} x_{k,j}$ . Then  $\mathbf{S} = (n-1)^{-1} \sum_{j=1}^{n} \mathbf{x}_{j} \mathbf{x}_{j}'$  or  $\mathbf{S} = (n-1)^{-1} \mathbf{X} \mathbf{X}'$ . So correlation patterns among genes are derived from XX'.

#### ♠ Matlab data input, exploration, summary, graphics