Supplemental Handouts for Simple Linear Regression (Ch. 7)

- page 1 Ecological correlations (Freedman, Pisani, Purves, Statistics)
- page 2,3 Regression effect/fallacy (FPP) + practice problems
- page 4,5 Plots of residuals vs. fitted values (Wiesberg, Applied Linear Regression
- page 6-8 Notes on diagnostics (Guenther Walther, STAT201, Stanford)

Outline, 1/13/04

- 1. Simple Linear Regression (SLR) estimation
- 2. Assumptions
- 3. Parameter estimation in SLR
- 4. Inferential tools: Illustrated using height/nematode example

```
Value Std. Error t value Pr(>|t|)
(Intercept) 10.3264 0.6890 14.9876 0.0000
Number.of.Nematodes -0.5738 0.1228 -4.6740 0.0004
```

Residual standard error: 1.933 on 14 degrees of freedom

Multiple R-Squared: 0.6094

F-statistic: 21.85 on 1 and 14 df, the p-value is 0.0003584

Questions to answer for nematode/plant height problem:

- (a) Is there evidence of a linear association between nematode level and plant height?
- (b) Does nematode level cause decreased plant heights? What info is needed to infer causality?
- (c) Are decreased nematode levels associated with increased plant growth?
- (d) What is the mean plant height when 0 nematodes are present? Estimate this mean and give a 95% confidence interval.
- (e) Give a 95% CI for the mean height when there are 5000 nematodes present. Hint: centering trick Solution: subtract 5 (x 1000) from each of the x's, and re-run the regression. In Splus, the formula is Y I(X-5). I() notation is used for transformations of x.

```
Value Std. Error t value Pr(>|t|)
(Intercept) 7.4575 0.4987 14.9551 0.0000
Center.Nematodes -0.5738 0.1228 -4.6740 0.0004
```

Residual standard error: 1.933 on 14 degrees of freedom Multiple R-Squared: 0.6094

Multiple k-Squared: 0.6094

F-statistic: 21.85 on 1 and 14 df, the p-value is 0.0003584

95% CI for mean plant height when 5000 nematodes are present: 7.458 + -t(0.975,14) (0.499)

- 5. Checking assumptions by looking at residuals
 - (a) Assumptions checked: mean zero errors, constant variance of errors
 - (b) Diagnose: nonlinearity, nonconstant variance, presence of outliers
 - (c) Reading: 5.5.2, p. 131; Display 5.6, p. 133; 8.3.2, p. 214; handouts
- 6. QQ normal plot of residuals, Reading: p. 224-225
- 7. Plotting residuals vs. time order (8.6.3), vs. spatial location